

Brain at work: time, sparseness and superposition principles

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1. ABSTRACT

Many studies explored mechanisms through which the brain encodes sensory inputs allowing a coherent behavior. The brain could identify stimuli via a hierarchical stream of activity leading to a cardinal neuron responsive to one particular object. The opportunity to record from numerous neurons offered investigators the capability of examining simultaneously the functioning of many cells. These approaches suggested encoding processes that are parallel rather than serial. Binding the many features of a stimulus may be accomplished through an induced synchronization of cell's action potentials. These interpretations are

supported by experimental data and offer many advantages but also several shortcomings. We argue for a coding mechanism based on a sparse synchronization paradigm. We show that synchronization of spikes is a fast and efficient mode to encode the representation of objects based on feature bindings. We introduce the view that sparse synchronization coding presents an interesting venue in probing brain encoding mechanisms as it allows the functional establishment of multi-layered and time-conditioned neuronal networks or multislice networks. We propose a model based on integrate-and-fire spiking neurons.

2. INTRODUCTION

2.1. Superposition principle

Deciphering neural code(s) is one of the most challenging tasks in contemporary neuroscience. Indeed, the understanding of brain mechanisms leading to a coherent perception of the sensory world has escaped us, in spite of enormous efforts dedicated toward this goal in the past century, although several research avenues have been investigated. The principles underlying neuronal information processing have direct implications on issues as diverse as the emergence of consciousness, or the engineering of efficient retinal or cochlear implants. This paper intends to provide a brief overview of the current knowledge concerning neural coding, with a focus on temporal codes, that is, time relationships between action potentials arising from different neurons. These time relationships led to the hypotheses of temporally sparse coding and superposition principle, or multiplexing. Temporally sparse coding occurs when few neurons are active at the same time, in millisecond time scaling. In that situation, the instant of firing of a neuron (or group of neurons) can encode information based on its timing with other groups of neurons. Groups having close timing take part in the same coherent activity to build a representation of stimuli by the superpositioning of layers of coherent feature neurons. This characterizes the “superposition principle.” Numerous experimental results supported this hypothesis and led to the claim that synchrony between action potentials arising from several neurons is related to sensory signalling. For instance, many authors (1-5) have described neurons in the cortex displaying sparse firing of action potentials and the time relationships between spikes across anatomically scattered neuronal assemblies, and they demonstrated that synchrony is an efficient means for information coding, allowing discrimination between stimuli (for additional supporting views see 6,7). It must be noted that the above view is challenged (8). For instance, Lamme et al. (9), found that synchrony was unrelated to contour grouping. Moreover, they suggested that rate co-variation depends on perceptual grouping, as it is strongest between neurons that respond to similar features of the same object. Others have reported no systematic relationship between the synchrony of firing of pairs of neurons and the perceptual organization of the scene. Instead, pairs of recording sites representing elements of the same figure most commonly showed equal amounts of synchrony between them as did pairs of which one site represented the figure and the other the background (10). Palanca and DeAngelis (11) concluded that synchrony in spiking activity shows little dependence on feature grouping, whereas gamma band synchrony in field potentials can be significantly stronger when features are grouped. Thus the debate is open and deserves a new insight.

For decades the modular architecture of the cortex has directed investigations towards a hierarchical model in which coherent perception rests on a cardinal unit that captures all local characteristics of an object, allowing its conscious perception (12,14). Such an organization is substantiated by cells responding selectively to face in the

temporal and frontal areas (15-17), is certainly inadequate for the perception of colossal number of stimuli presented to the sensory systems (5). Yet, it has been postulated that categorical objects evoke discharges in neurons that form clusters, even thought categories are rather broad such as animated vs inanimated (15). The modular organization of the cortex rests on the principle that cells sharing similar properties are grouped together within functionally defined columns or domains. (18-20). Interestingly, it has been reported that neurons of temporal areas signaling crude figures such as stars, circles and edges excite distinct clusters of cells (21,22). In the visual system of humans (23) lesions of the area MT severely impairs motion perception, whereas lesions of area fusiform and lingual gyri elicit a lack of color vision. In these subjects the world is colorless while motion is well perceived. Hence one single target elicits responses in a large number of separate cortical areas whose cells are encoding only a partial aspect of a single visual image. Therefore, neurons responding optimally to the same features or coding for adjacent points in visual space are often segregated from one another by groups of cells firing maximally to different features. Consequently, such a scattered grouping requires an integration of these neuronal activities to achieve coherent perception.

Many basic processes for encoding sensory environment have been thoroughly investigated during the past several decades; several are summarized in the following sections.

2.2. Conventional rate coding

In rate code mode, the information is contained in the number of all-or-none action potentials, or spikes, in a given time interval. For instance, the classical functional relationships between the axis of orientation of a moving edge and the firing rate are the basis for establishing tuning curves for orientation selectivity. Indeed, most neurons in the visual cortices are rather narrowly tuned across several dimensions such as orientation, length, wavelength, speed, size, contrast etc. (24). However, the situation is rendered more complex by the observation that in monkeys many neurons respond to conjunctions of properties, for instance: orientation, motion and color (22,23,25). Along this line, Tanaka (26) has shown that neurons clustered in modules or columns in the temporal cortex, are discharging to the presence of a combination of features sharing at least a few common traits. These clusters of cells are identified as “object-tuned cells” (or contour-tuned), although objects are relatively rudimentary (21,22,25). As a result, according to the rate code hypothesis the cortical neuron may be considered as an integrating and firing device (13, 27) because it is the firing rate modulations that signal differences in image properties.

Several problems were, however, raised regarding the above proposition. We shall summarize the most critical. In general, cells in areas occupying higher levels in the processing hierarchy are often less selective for specific features, that is, they respond fairly well to several features of applied target. No object-exclusive neurons have ever been reported. Such cells should be

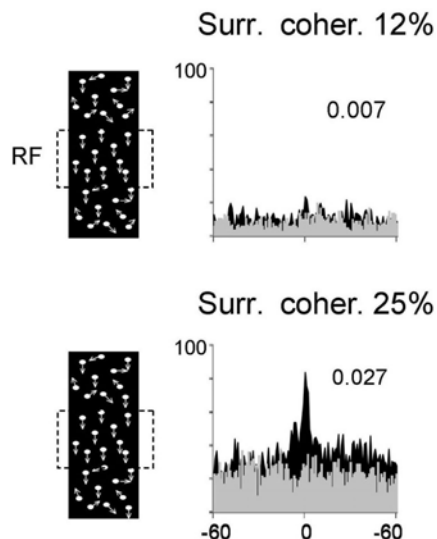


Figure 1. Two examples of cross-correlograms produced by random dots stimuli positioned in the surround above and below of the receptive field (RF), both RF (partially superimposed) are delineated by square. Upper, 12% of dots in the surround are moving in the same direction as dots within the receptive field. This induces a weak insignificant central peak. Lower, 25% of dots in the surround move in the same direction. This higher proportion induces a robust central peak at 0 ms time lag signifying synchronization. X-axis: ms, Y-axis: number of events. Gray areas cross-correlograms are obtained following shuffling; this procedure shows flat cross-correlograms. Left panels are schematic representation of the stimuli, random dots. Number in inserts: synchronization magnitude computed as in reference 58.

located in an ultimate area of convergence, which should be quite large in size to contain the extraordinarily large number of cells required to encode all targets potentially to be shown to the sensory systems. Nevertheless an attempt to localize and identify such neurons ("Grandmother cells") was performed by Tanaka et al. (15,26) using promising imaging techniques, accompanied with more classical electrophysiological recordings. They report grouping of cells along some quite rudimentary properties such as contours. In the olfactory system any one neuron is a poor predictor of odorant identity (28). These cellular properties seem too basic to allow a subtle discrimination of local characteristics that identify an object. Furthermore close properties often evoke more or less equal firing rates, hence the rate code is ubiquitous and may lead to confusion (29).

2.3. Oscillations for Coding

Oscillatory rhythms of theta, alpha, gamma, frequency ranges are hypothesized to reflect key operations in the brain (memory, perception, etc.). One hypothesis states that a non stimulated brain (brain at rest) exhibits oscillations in large networks of oscillatory neurons. A stimulation is then a perturbation of this oscillatory mode (2, 30, 31). It is assumed then that a strongly stimulated

brain disrupts the rhythm at rest and exhibits periods or epoch of sparser oscillatory synchronization. Instead of relating firing rates as a mean of signalling image properties at the neuronal level, it has been suggested that the rhythm of the evoked discharges could be better suited to signal target characteristics.

In fact it has been proposed that within the gamma range (20-100Hz) a definite frequency may be distinctively associated with some properties. A precise frequency would be the tag identifying a particular feature of an object. Along this line gamma oscillations are also stimulus dependent and are considered to be an "information carrier" (32-43). The examination of gamma activity reveals two gamma components which may subserve two different information-processing functions. Early "evoked" gamma oscillations tend to be time-locked to the stimulus and may primarily be an index of attention (44, 45). By contrast, the later induced gamma response tends to be loosely time-locked and serves a context processing and integration function. Others (46) suggested that pyramidal cells with long range connections (ascending, descending, and lateral connections) might operate to achieve synchrony or time coordination between separate sites of receptive field inputs (47-49). Recordings of gamma rhythms from humans scalp have shown that gamma oscillations emerge at or above the psychometric threshold suggesting that these rhythms may be linked to brain processes involved in decision making (39). In addition, synchronized activity has been associated with phase correlation between neuronal oscillations in gamma range. Attended sensory stimuli facilitate gamma synchronization which increases perceptual accuracy and behavioral efficiency (50). Extending this role to neural computation, these authors suggested that there is a selection of neurons contributing to sensory input transmission. It must be emphasized however, that synchrony and induced gamma oscillations are two distinct processes since we can record synchrony without oscillations and vice-versa (51, 52).

2.4. Time correlation code: synchronization

Milner (111) and Malsburg (4) advanced an alternative hypothesis. Neurons sharing sensitivity to similar characteristics exhibit synchronous action potentials allowing coherent perception (5, 12, 53-62). More generally, this proposition implies that neuronal signalling rests on time relationships between spikes fired by different and distant neurons. Synchrony will be the acute situation when action potentials of different neurons occurs simultaneously within a 1ms time-window.

Since synchronization involves the participation of many cells it is assumed that the synchrony creates a coding neural assembly allowing the linkage of a constellation of local features (such as colors, angles, motion, direction, etc.) into one coherent picture. Experimentally, the synchrony is disclosed by a central peak when the evoked spikes of two trains are time cross-correlated (57-60). This central peak occurs within a very brief epoch (1 to 5 ms), which reduces the probability of accidental coincidence. (see example in Figure 1). The

magnitude of the central peak is stimulus dependent, that is, units with spatially separated receptive fields fire synchronously in response to objects sharing common features (for instance light bars moving in the same direction, or having same orientations) but asynchronously in response to two independently moving objects (36). Similar data were reported in many species and other sensory systems (20, 63, 60, 63, 64). Yet there is no reason to postulate that targets moving in opposite directions or dissimilar features are less coherent than targets moving in the same direction or sharing similar features. Therefore, any feature belonging to the same object may lead to synchronized activity. Such coding through synchronized activity has been called a neural distributive system. It has also been called linking fields, or binding assemblies (65). Abeles (13) inspired by Hebb (66) developed a radical new concept that the unit of information transmission in the cortex is a synchronously firing group of neurons (synfire group)(Figure 1).

2.5. Coherent and non coherent stimuli

Globally, these neurons will create sparse networks that are superimposed. One neuron can contribute to two neuronal assemblies firing at different intervals or different time lags. These neuronal assemblies of spiking cells implement segmentation and fusion that is the integration of sensory objects' representation. Although network sparse coding allows signaling of a few trigger features of an object, for instance, a mixture of colors AND orientation. Still it may be insufficient to account for sudden and rapid variations in time and space. Hence, we put forward multilevel sparse networks, or a superposition of neuronal assemblies such as parallel sets of assemblies rather than serial or successive formation of assemblies in a hierarchical stream. The superposition principle or multiplexing allows that several assemblies may be simultaneously active and each member is free to leave one assembly and join another one if the collection of stimuli is modified. Considering that synchrony occurs in the few milliseconds range the formation of several assemblies is rapid, transient and linked to one particular stimulus, and only refractory periods of individual neurons may be a limiting factor. This principle is illustrated in Figure 2.

However, under proper conditions any cell may join other sub-networks because the binding is dynamic and changes with time. It should be noted that inputs do not need to be similar but they need to belong to the same object hence applied at the same time.

2.6. Dilemma

There is, however, a conceptual dilemma. In the literature it has been reported that synchrony is mostly induced if visual targets share similar properties such as direction or axis of orientation. Yet, a priori and as mentioned above, there is no reason to postulate that two targets moving in opposite directions are less coherent than targets moving in the same direction. And indeed in support of this latter statement we have shown that images with fractures, orientation disparities or angles induce synchrony (42). Nevertheless, the binding-by-synchrony

hypothesis is flexible and dynamic as cells of an assembly may quit, that is desynchronize, and other neurons may join, that is synchronize, depending on image modifications, thus signifying image properties. In addition synchrony across spike trains operates over large separations between cortical areas.

2.7. Problems with Correlation Hypotheses

In spite of the above-mentioned attractive properties, the correlation hypothesis is not immune from weaknesses (7, 10, 29, 37, 57, 67-73). We shall summarize the most important difficulties. Assuming that synchronization is the vehicle for signalling, then neural populations should be functionally bound together. But are anatomical connectivity and receptive field properties related? How can neurons engage in stimulus induced synchronous interactions with a subset of their inputs when a large percentage of all cell inputs are also active and often spontaneously synchronous? How are synchronization and oscillations computed and read out in the presence of stimuli?

From the above brief review it seems clear that both the serial or hierarchical and the distributive models fall short of explaining the encoding processes of neuronal signals. Therefore more needs to be considered. We show in the following sections that neurons respond to subsets of their inputs. Inside a subset, the activity is synchronous therefore; a neuron receives a time multiplexed subset of activity.

3. SPARSENESS AND MULTIPLEXING

The above brief review calls for supplementary models that may play a role in elucidating the encoding processes carried out by the brain. A body of recent experimental and theoretical data (74) seems to point towards a parallel and distributive organization of neuronal activity.

Although the number of brain neurons is barely imaginable, cells are relatively quite, that is their firing rate is modest (range ~3-5 Hz) (75). It has been suggested that less than 1% of cells are active at any given time (76) because of the high metabolic cost of action potential. Yet one per cent of neurons of a given population are still a fairly large number. The situation is further complicated by the fact that the number of action potentials evoked by the same stimulus varies considerably from trial to trial even though the target is rigorously identical. In addition, two neighbouring cells presumably sharing similar properties react in quite opposite fashion.

3.1. Responses of single cells are variable

Traditional experiments, in which a microelectrode is implanted in the visual cortex to record single neuron firing evoked by a rather simple stimulus constituted by a dark light edges or a sine-wave grating drifting across the cellular receptive field, reveal that cellular responses vary considerably from one trial to the next, within a time frame of a few seconds. In the example of Figure 3 each curve represents an orientation tuning

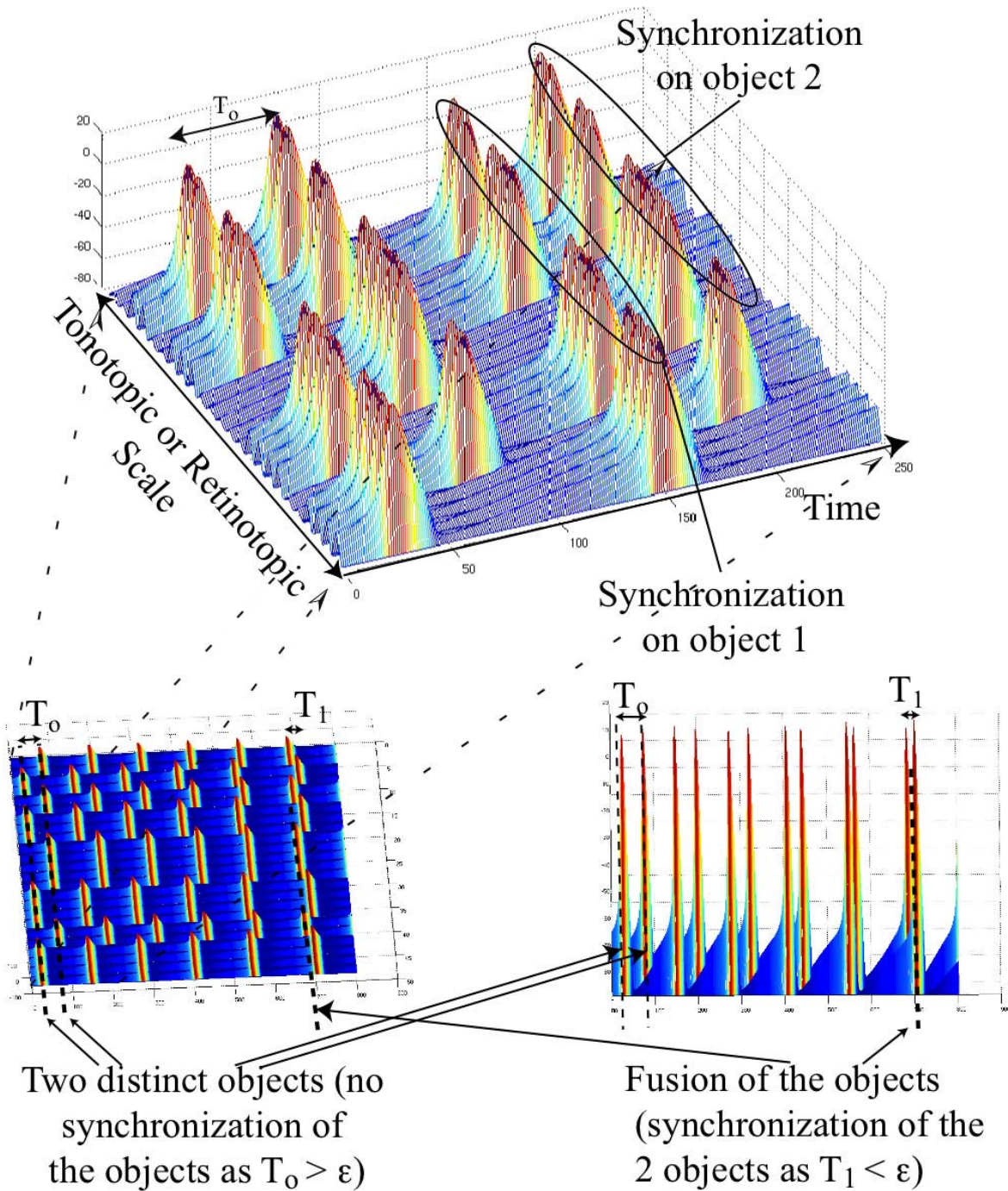


Figure 2. Illustration of temporal binding with 24 simulated neurons. In this example, neurons are distributed according to the tonotopic organization of the auditory system. But the same principle holds with a retinotopic organization of vision. Neurons 1, 2, 3, 4, 7, 8, 9, 10, 16, 17, 18 and 21, 22 are synchronized and fire at almost the same time, as their input stimulus is dominated mostly by auditory object 1 (102,103). These neurons are bound according to the temporal correlation principle. In this example the other neurons are bound to another auditory object. Segregation of the information is done in the time domain (timing of the neurons) and fusion is performed by the binding (synchronization of the neurons). Second row of the Figure shows how the 24 neurons can dynamically synchronize or desynchronize to segregate two objects or to fuse into one object based on the timing of the neurons. This mechanism allows a rapid change in the binding. T_0 is the time difference between two unsynchronized set of neurons. T_1 is the maximum time difference tolerance for two sets of synchronized neurons.

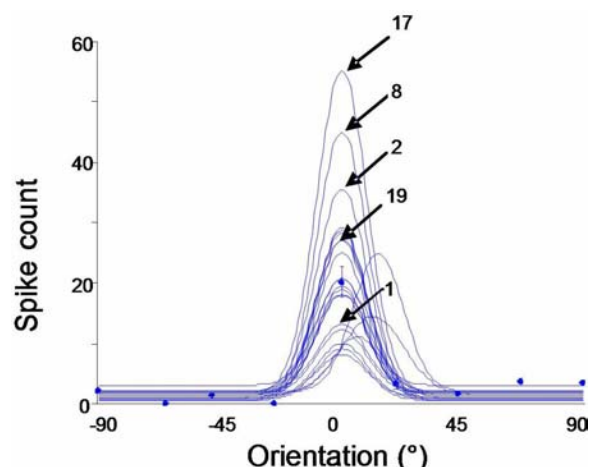


Figure 3. Responses are unpredictable. Twenty five successive stimulations. Stimulus duration of 4.1 sec. Inter-trial interval 1-3 sec, random. Twenty five tuning curves are shown each fitted with Von Mises's equation. Although the optimal orientation (0°) remains the same, the magnitude of the discharges changes considerably in spite of the fact that the stimulus is exactly the same. Number: order of the presentation. X- axis Orientation in degrees, Y- axis firing rate (spike count) Number pointing a few peaks indicate the order of this particular presentation. Magnitude of responses does not change regularly in relationships with the presentation number.

curve as fitted accordingly to Von Mises's equation (total number of presentation 25).

Although all physical properties of the stimulating sine-wave patch are identical for every presentation, the firing fluctuates considerably regardless of the order of presentation and hence is unpredictable (see Figure 3). This variability between trials is an important issue because the neuronal processing is carried out for every trial as it is unlikely that the receiving neuron average firing rates (as commonly done with PSTH). A consequence of such variability is that the unit at the next stage receives an input whose strength is variable. Several experimental data support this, for instance the peak of the firing rate is unrelated to the stimulus energy (light intensity in this example). Yen et al., (77) made the stimulus more complex by presenting natural scenes and demonstrated that responses of adjacent neurons in cat striate cortex differ significantly in their peak firing rate when stimulated with natural scenes. The heterogeneity of responses in unanaesthetized monkey suggests that V1 neurons upon stimulation of classical and non classical receptive fields responded in a very selective fashion (78). Such high selectivity in turn augments the sparseness of the population of active neurons. The direct consequence of the above results is that individual neurons carry independent information even when they are situated in the same area such as an orientation column. It may be concluded that individual neurons carry independent information (see below). It must be kept in mind however that averaging responses of many responsive cells produce at population level stable averaged activity. In addition not identical

activity does not necessarily imply that cells are independent of each other. Yet commonly these responses are added with the aim to obtain an averaged firing rate. Since average masks variance specific to each stimuli presentation, averaging prevents coding contained in the event-to-event variances. Nevertheless it has been proposed that this variance is not noise but a signal with encoding values. Furthermore a computation of the response fluctuations suggests that an extremely small proportion of afferent action potential may be associated with the large variance in spite of usually large numbers of afferent axons (79). Yet such processes based on variance do not disqualify encoding through time relationships between spikes. The author postulates then that sparse coding allows for the reduction of number of active fibers (79). Then in order to increase reliability of the signaling, synchrony of action potentials may strengthen the encoding activity, particularly when stimuli contain dissimilar trigger features. This is particularly relevant when evoked discharges have different magnitudes in response to two successive stimuli presentations. It is conceivable, that while neuronal firing may vary the synchrony level may remain rather constant. In addition we have shown that few synchronizing cells are sufficient to increase signaling power (80) (See below) In spite of a large number of synaptic inputs connecting to a neuron, a small number of synchronized inputs may be sufficient to significantly activate post-synaptic cells. Hence a process that allows increasing the coding potential may be synchronization. The functional gain is that one keeps the number of inputs small but there is an increase of the strength of synaptic transmission.

3.2. Modulations of responses of neighboring cells

The spike sorting methodology offers substantial advantages when recording neuronal activities. Indeed this technique is based on the ability of the recording system to capture action potentials from a small area and then sort out individual spikes. In general, spikes generated within a 50-100 microns radius may be collected reliably (81). Hence several cells that are close to each other and very often belong to the same functional domain such as same orientation column may be sorted out from the neuronal cluster under the tip of the electrode. In spite of this proximity, neighboring cells display quite different behavior. For instance, Tan et al., (82) showed that two neighboring cells of area 17 of cats sharing the same preferred orientation exhibited opposite response modulation when a remote target was added outside the classical receptive field. One cell reacted with an increased firing rate while the companion cell discharged at a lower rate. (See Figure 4)

Additional investigations have disclosed that adjacent cells display heterogeneous selectivity to spatial frequencies, for instance a low pass cell is adjoining a band pass cell (83, 84). Such disparate distributions of neurons with different sensitivities are quite common in polysensory areas where different sensory modalities converge on single cells. The neuronal reactions are even less homogeneous amongst units belonging to small clusters. The above survey points to a rather small

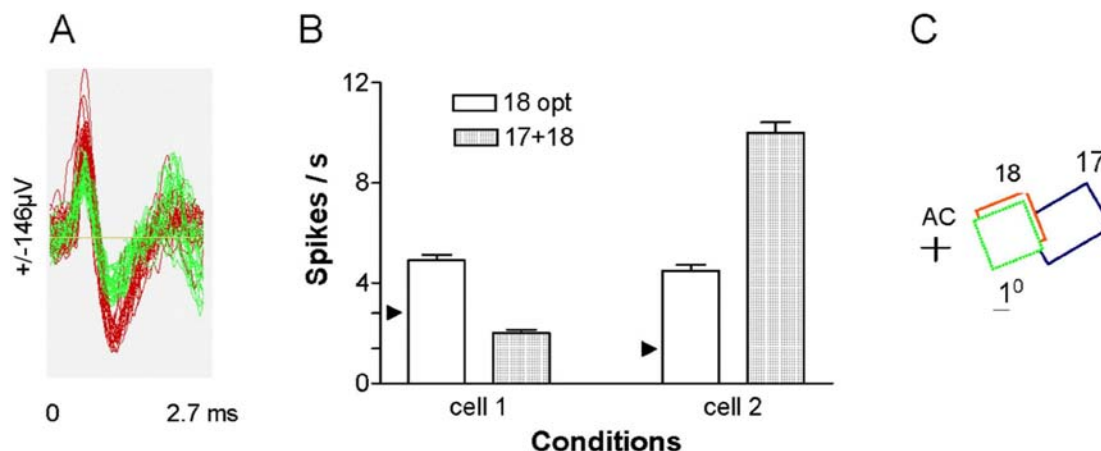


Figure 4. Neighbouring cells behave differently. Two neurons are sorted out from the same tip of the recording electrode positioned in area 18 of the cat. Cells are color coded (red and green), respective receptive fields are shown in C. Both units have similar optimal orientation. If an additional target is positioned in the receptive field of the cell in area 17, as shown in C, the cell 1 (red) diminishes its firing rate, while the companion unit (green) augments its firing rate. The modulation of responses is shown in B: receptive fields in area 18 are stimulated in isolation, optimal parameters: orientation of sine-wave gratings (opt). 17+18 both cells are simultaneously stimulated by separate sine-wave patches. AC: area centralis. This figure shows that although both cells share orientation domain and are located in very close proximity they react in opposite fashion when additional target is introduced in the visual field. Modified with permission after Tan et al., 2004.

subpopulation of neurons within a limited cortical area that are active during a determined time window.

Similar mixed properties within a small cluster of cells were reported for other sensory modalities. For instance, in the olfactory system it has been demonstrated that both Kenyon cells and the neural circuitry interconnecting the antennal lobe and the mushroom bodies favor the detection of synchronized spatial-temporal patterns that are induced in the antennal lobe. This would allow the tuning of the code for odor identity (74, 85, 86). Therefore, it seems that it is the interactions among neurons in brain circuits that underlie odor perception in the locust. In the auditory system cortico-cortical fibers connect cell groups with large difference in characteristic frequencies, sometimes over one octave and non-overlapping receptive fields. Such heterotopic interconnections allow binding highly composite sounds stretching over large frequency spectrum (87).

The above observations do not exclude the well confirmed classical columnar and modular organizations that are characterized by classes of neurons responding to similar properties of sensory inputs. In spite of that, the modular organization does not rule out the fact that only a small proportion of cells within a column or a cluster may be simultaneously active at any moment and furthermore the neighboring unit may behave in a different fashion due to local interneuronal interactions. In support of the above statement *in vivo* two-photon calcium imaging demonstrates sparse patterns of correlated activity. In particular there is little dependence. It is suggested the existence of small clustered or intermingled subnetworks within few cells are co-active (88) Furthermore adjacent sub networks may have distinct preference identity. The

dissimilar activity between neighboring cells may be attributed to several organized overlaying maps in the same region such as fine-scale retinotopy, ocular dominance, spatial frequency. Such parcellation leads to sparseness concept.

3.3. Sparseness

Up to this point we have expressed the view that individual neurons fire with a different rate to identical stimuli, or to different properties even though they belong to a single functional domain. We have also described that nearby units behave electrophysiologically in a different fashion. In addition within any given time window (relatively short) cellular activity is low even after stimulus application and the number of active cells is small. In addition it has been suggested by many that the firing rate of a neuron is a poor predictor of the property of the applied stimulus. This pusillanimity of activity introduces the concept of sparse coding (73, 78, 89-92). One must distinguish sparseness of the response of a neuron to some features of a stimulus from sparseness of a functional neuronal network. Therefore there are two distinct definitions of sparseness. The “lifetime sparseness” refers to the variability in the response of a single neuron for instance when a succession of frames of natural images that make up a movie are projected to the visual system. This aspect has been dealt with earlier. The “population sparseness” is defined as the response variability within a population of neurons for each single frame that is presented (89). This second level of analysis shall be discussed and illustrated below. We will now turn to the theme of examining the time relationships between action potentials emitted by two (or more) neurons that may be located at various distances.

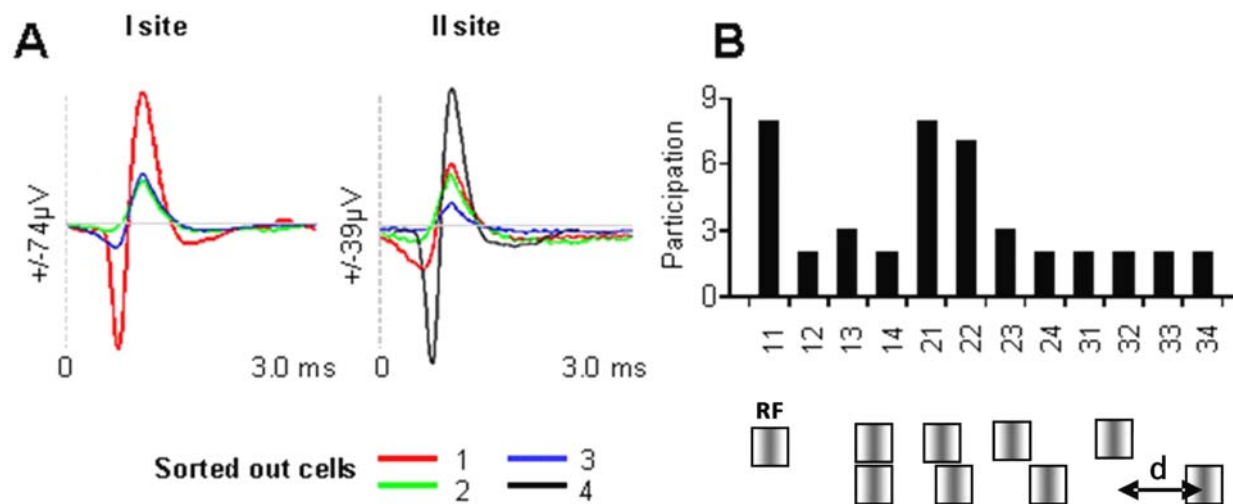


Figure 5. Synchronization is selective to image properties. In A, action potentials are sorted out from two sites in the visual cortex (distance ~ 400 microns). Three cells in site I and four cells in site II. Cells are color coded. The image (see in B under histogram) is constituted by two identical sine-wave patches (spatial and temporal frequencies, velocity and direction optimized to evoke strongest response from the compound receptive field). The lower patch is displaced laterally in steps. Hence, the parameter that distinguishes images is the distance d separating both patches (0.5, 1, 2, 4, 8, 12 deg., center to center). Total number of configurations applied randomly: nine, compound receptive field stimulated in isolation, patches aligned, peripheral patch alone without the central patch (only five configurations are displayed in B, lower row). In B, after shuffling, synchronizations are computed between pairs of cells, pairs are identified by numbers on abscissa. Participation indicates the number of images producing significant level of synchrony (Z score > 4), for instance pair 1-1 synchronized for most stimuli (8/9), whereas synchronization between cells 1 and 2 was quite selective since only two image configurations evoked significant synchrony.

Few neurons have the same selective receptive field, as suggested above, sensory information is represented by a relatively small number of simultaneously active neurons out of a large population. Such sparseness of neuronal activity may seem counterintuitive considering brain imaging data where whole cortical areas are activated by a given stimulus. However, one has to bear in mind that most imaging techniques are indirect, that is, based on hemodynamic changes rather than neural activity. Moreover, those techniques reflect mostly synaptic (neuronal computation) and inhibitory activity is seldom dissociated from excitatory activity (93). On the other hand, sparseness is somewhat instinctive to electrophysiologists, since one can lower an electrode in the cortex without detecting any stimulus-responsive cell (within the limits of the tested stimulus features range). Even when using multiple electrodes the number of active neurons remains small in relation to the cell population sitting under the electrode's tip.

3.4. Sparseness in the coherent firing: Time relationships between action potentials

We will now focus on the time correlation hypothesis. A previous study (80) measured the level of synchrony between two populations of cells and compared the magnitude of synchrony in relation to image structure (Figure 5).

Two sine-wave patches are applied in the visual fields. A central patch covered both receptive

fields of two pools of cells while a second peripheral patch had a variable distance from the central patch. Hence only the distance between both targets was the characteristic that differentiates various presented images while other properties (size, contrast drift speed and spatial frequency) remained unchanged. In total nine configurations were tested (see legend).

The histogram of Figure 5 indicates the frequency at which time correlations performed between cells recorded in both sites (three cells in site I and four cells in site II) produce significant synchrony. The twelve pairs are identified by numbers labeled in X axis of the histogram of the Figure 5 B. This distribution shows that only pairs 1-1, 2-1, 2-2 exhibited significant synchrony for most (8/8 and 7/9) conditions ($SI > 0.012$), whereas the remaining pairs synchronized significantly only for a small number of configurations of the image applied to the visual field. This distribution suggests that neuronal assemblies formed by synchrony are rather selective (94). The above results point towards one considerable advantage not shared by other models. Since one assembly is formed for one particular stimulus configuration or set of stimuli, it allows achieving a high degree of selectivity which in turn precludes ubiquitous situations in which several trigger features evoke comparable responses from single neuron. The versatility of neuronal assembly is further discussed in the next Figures.

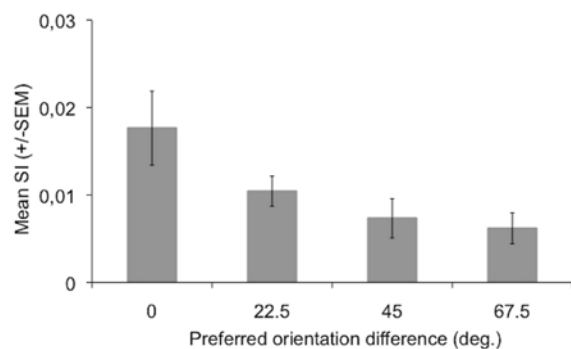


Figure 6. Synchrony index (SI) measured in relation to orientation differences between two groups of cells. Orientation is indicated in degrees on the X axis. The closer the orientation, the higher the synchrony index (SEM: standard error of the mean).

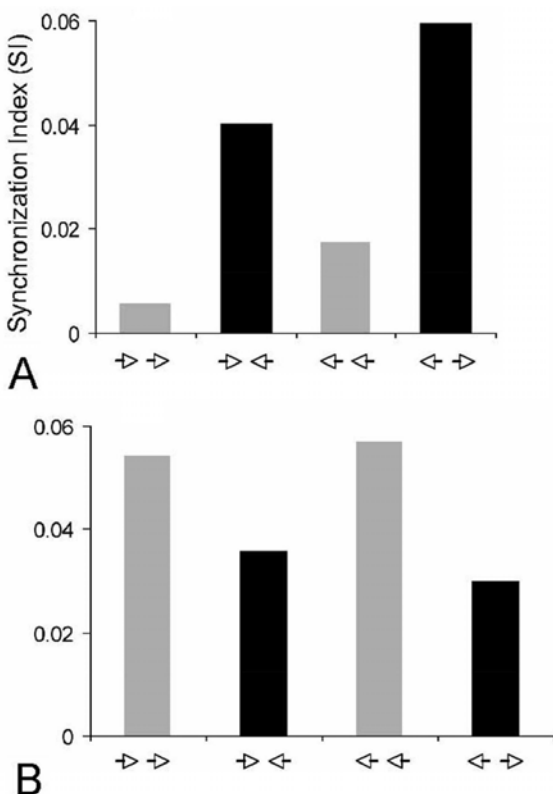


Figure 7. Synchrony depends on the direction of motion. Two sine-wave patches are positioned in respective non-overlapping receptive field. Each sine-wave patch evokes the optimal responses from cells. In A opposite motions (collision or divergent directions) produce higher synchrony indexes than parallel motions. In B the opposite is shown. X-axis: arrow heads motion direction; Y-axis: synchronization index

In Figure (Figure 6) we show that the synchrony magnitude is increased as the orientation difference between two cells becomes narrower. Conversely the wider the difference the smaller the synchrony index between the

two cells. Comparable results were reported elsewhere (7, 37, 55). This result suggests that similar features lead to more frequent action potential coincidence, providing thus a substrate for the formation of encoding assemblies by synchrony. On the other hand such data hinder strong synchronization when features are dissimilar yet belonging to the same image such as targets including cross orientation features of a picture frame. Yet as mentioned previously there is no reason to postulate that disparate targets are less perceptually coherent, for instance parallel motion in opposite direction. Others have suggested that synchrony may potentiate collinear contour synthesis because cells may synchronize within and across different orientation columns (95)

In next Figure (Figure 7) we illustrate data showing that some pairs synchronize better for parallel motion while another pair exhibits more robust synchrony if gratings are drifting in the opposite direction. The example of Figure 7 compares synchrony levels when drifting directions of two sine-wave patches are in opposite direction (collision or divergent motions) with parallel motions. In A the synchrony index is of higher magnitude for opposite direction whereas when the same stimuli move in the same direction (right or left) the synchrony index is much weaker. In B another pair shows the opposite pattern, that is, parallel motion induces a better synchrony. Altogether, these results suggest that it is possible to achieve synchrony for many characteristics of applied images. Thus, it is unnecessary to call upon a coherency to establish a coding assembly by synchrony. It is worth underscoring that in many of the above studies the firing rate does not change while synchrony magnitudes follow image modifications.

The consequent formation of such assembly is that a few synchronizing cells may suffice to encode one particular target which in turn lead to the sparseness concept because a relatively small number of units are simultaneously committed to encoding a selected number of optimal trigger features. The sparseness or superposition/multiplexing organizations are two notions that complement each other.

Duret et al., computed the coefficient of determination and compared the synchrony degree between single pairs and multiunit recordings from which individual cells were sorted out (80). The study showed that correlating pair wise the neuronal impulses of single cells may produce a synchrony whose magnitude equals the synchrony level produced by correlating multiunit recordings that comprise a much larger number of cells (including the two tested cells initially) and evoke a much higher rate of excitation. These results suggest that for some configurations two synchronizing neurons suffice to signal reliably a target. Such a small number of cells is compatible with the desired scaling-down of neurons involved in brain functions. At population level, cells expressing weaker correlations are contributing to encoding but likely with smaller weight. However, apart from theoretical and computational considerations, the theory of sparse coding is based primarily on two observations:

neural silence, and the cost of cortical computation. Neural silence refers to the fact that neurons fire action potentials rarely or only to very specific stimuli (99). Many investigators reported that recordings in various parts of the cortex detect substantially less neurons than expected on anatomical grounds (100, 101). In the auditory system Eggermont showed that within a cortical column neurons fire synchronously on average about 6 % of their spikes in a 1ms bin (20, 87). Yet such small proportion of time correlated activity is sufficient for cortical reorganization following experimental manipulation (89). This conclusion is further supported by Petersen et al., (102). Analyzing time relationships between spikes, they suggested that small number of neuron is able to support the sensory processing supporting complex whisker-dependent behaviors.

To summarize, it appears that at the single cell level the variance of excitability of neurons to identical stimuli poses the risk of ambiguous encoding while the large variations responses modulation of neighboring cells indicate that a neuron, even when belonging to the same functional domain, operates in a relatively independent fashion. This last assertion does not rule out cross influences between neurons belonging to local networks. Yet, coding stimuli features through an assembly of cells that synchronize their action potentials offers the advantage of signaling specific features with less ambiguity. The uncertainty is reduced because only cells excited by specific features are active and in addition the assembly is structured by the time relationships of the respective neurons that lead to perception. Cells lacking such time relationships lose their transient participation in the coding assembly. This in turn, further reduces the number of units belonging to a putative encoding group and hence the noise is further diminished. Finally, since the time relationships, such as synchrony, arise in a very short time window sometime within 1 ms, the establishment and destruction of such an assembly is rapid and it also allows the creation of several multiplexed assemblies, that is, a superposition of several coding assembly allowing flexibility in the representation of several stimuli present in the subject's sensory space.

3.5. Conventional sparseness measures

In previous section we defined sparseness which implies that few active neurons should enable reliably coding of stimulus. Now we introduce some measures that are used to evaluated the degree of sparseness in a neuronal network. Let us assume that a population of N neurons has sparse activity which is to be measured (as we are interested in comparing the sparse activity between networks). We designate by r_i the electrical activity of a particular neuron i from the considered population. One common sparseness measure for a population of N neurons is the L_α norm (sometimes called the L_p norm):

$$\|r\|_\alpha = \left(\sum_{i=1}^N |r_i|^\alpha \right)^{\frac{1}{\alpha}}$$

where $\| \cdot \|_\alpha$ denotes the norm and α is less than 1 when looking for sparse activity in a network of N neurons. r_i is the activity of neuron i (firing rate, firing rate minus the spontaneous firing rate, etc.). The smaller the value of L_α norm, the greater the sparseness. Kurtosis is another measure of sparseness. The normalized Kurtosis (i.e., Kurtosis excess) is defined as follows

$$K = \frac{E[(r_i - E[r_i])^4]}{\sigma^4} - 3 \quad (1)$$

where $E[\cdot]$ is the statistical average of variable r_i and σ is the standard deviation. K equals 0 for any Gaussian distribution. It is commonly used to evaluate sparseness as it characterizes the shape of the statistical distribution. For instance if $K > 0$ the distribution is said to be super-Gaussian (peaked shape); if $K < 0$ the distribution is sub-Gaussian (flat shape). This definition of flat or peaked shape is relative to the Gaussian distribution where $K = 0$. The greater the K , the sparser the distribution (the histogram of the distribution exhibits smaller frequencies for the greatest r_i values).

Another measure, used by Treves and Rolls (99), is more appropriate to neural data analysis. It is the ratio between the squared statistical average and the variance:

$$a = \frac{(E[r_i])^2}{E[r_i^2]} \quad (2)$$

One estimator of this measure is

$$\hat{a} = \frac{\left(\frac{1}{N} \sum_{i=1}^N r_i \right)^2}{\frac{1}{N} \sum_{i=1}^N r_i^2}$$

A small value of a characterizes sparse activity in the network (if the variance is large compared to the squared mean, then neurons have a different behavior for different stimuli). r_i can be the firing rate and N the number of neurons in the network.

The above measures are used by researchers to understand or to model sparse neuronal activity (or sparse organizations in the brain). In most of these studies the key variable is the firing rate of neurons (or averaged firing rate of groups of neurons). It is known that the timing relationships between spikes in some areas of the brain is

also crucial to encode information (see previous sections). Therefore, we propose that sparseness should also be examined in the context of synchrony between action potentials of pairs of neurons (or even between populations of neurons). In this new context, the sparseness computations described previously are still valid but instead of using the firing rates r_i we suggest the use of a synchrony magnitude (or synchronization factor) $S_{i,j}$ between neurons. Depending on the nature of the synchronization the index i, j designates a pair of neurons or two groups of neurons. For instance, the Rolls and Tovee (99) estimator becomes

$$a_{sync} = \frac{(E[S_{i,j}])^2}{E[S_{i,j}^2]} \quad (3)$$

A small value of a_{sync} indicates that only a few pairs of neurons (or groups of neurons) are synchronized at a specific time t while a high value shows that most pairs are in synchrony at time t . For a small a_{sync} the probability that different pairs of neurons are synchronized is low. For a greater a_{sync} , the probability that groups of neurons fire at the same time is greater.

3. THE SUPERPOSITION MOSAIC PRINCIPLE: SPARSNESS, SYNCHRONIZATION AND BINDING

We introduce in next sections our view towards a more complete model of the superposition principle based on sparse synchronization. Also, means to create a sparse neuronal representation with synchronization is explained below.

4.1. Synchrony for a sparse representation

At initial stages extraction is performed by the peripheral organs of the sensory systems. Coding locations or broad band-pass frequencies are possible at this first stage of the processing. For example, retinotopic organization in the visual system allows placing objects in an appropriate retinal register. The retinotopy is then conveyed to higher levels. For sound frequencies, tonotopic organization in the auditory system begins at the basilar membrane of the cochlea. However, at these peripheral levels of processing the neural activity is not very sparse as many neurons respond to various applied sensory targets with variable strengths since tuning curves may be relatively broad. Also, the coding is likely to be mostly based on the firing rate of neurons.

Then, after 3 to 4 synapses upstream (from the peripheral organs), neurons fire more sparsely with more independent responses. The relative decline of neuronal activity may be attributed to reciprocal lateral inhibition between parallel ascending streams. As an example, in the Inferior Colliculus the neural responses are relatively well

correlated with the auditory stimuli while in the auditory cortex responses are more sparse and neurons may fire in response to complex sounds (100). Interestingly, Bruno and Sakmann (101) have shown in rats that thalamocortical synapses have low efficacy as one action potential yields a very weak post-synaptic response. They also have shown that convergent inputs are numerous and synchronous. Hence cortical cells are driven by weak but synchronously active thalamocortical synapses. Their work suggests that, at this level of the brain, synchronization is a key aspect of the information processing. A large number of output neurons can elicit a strong post-synaptic response only if their afferents are conveying action potentials in synchrony. Then the inputs are highly correlated while the outputs are more independent.

Since synchrony of activity between neurons is related to stimulus properties, it seems logical to postulate that such binding by synchrony is less than ubiquitous. Indeed, only cells that are excited by specific features can potentially synchronize. The formation of such a neuronal assembly is specific to specific combinations of properties. As a consequence the feature extraction is facilitated. Figure 8 is a schematic representation of a hypothetic transformation from periphery to the central nervous system with a change in the coding scheme. We assume that at the peripheral level a place topological coding occurs while at the central system a sparsely synchronized coding is dominant. The set of M neurons can be dynamically divided into subsets. These subsets are comprised of neurons that are bound via synchrony.

Vinje and Gallant (78) have shown the existence of sparseness in the brain. Willmore and Tolhurst (103), Waydo et al. (104) and other authors have suggested that sparseness is a characteristic of the brain and describe its measure.

4.2. Sparse synchronization of oscillatory neuron

As discussed in the first section of this paper, oscillatory rhythms in the ranges of theta, alpha, gamma, frequencies are hypothesized to reflect key operations in the brain (memory, perception, etc.). One hypothesis states that a non stimulated brain (i.e. brain at rest) exhibits oscillations in large networks of neurons. A stimulation leads to an alteration of this oscillatory mode (29). It may then be assumed that a strongly stimulated brain disrupts the rhythm at rest (2) and we hypothesize in this paper that brain exhibits periods or epochs of sparser oscillatory synchronization.

5. A MODEL OF SPIKING NEURONAL NETWORK FOR BINDING WITH A POTENTIAL FOR SPARSE SYNCHRONIZATION CODING

In this section, we present a model of a network of spiking neurons that can be used to build a simulated binding neural network based on the superposition principle.

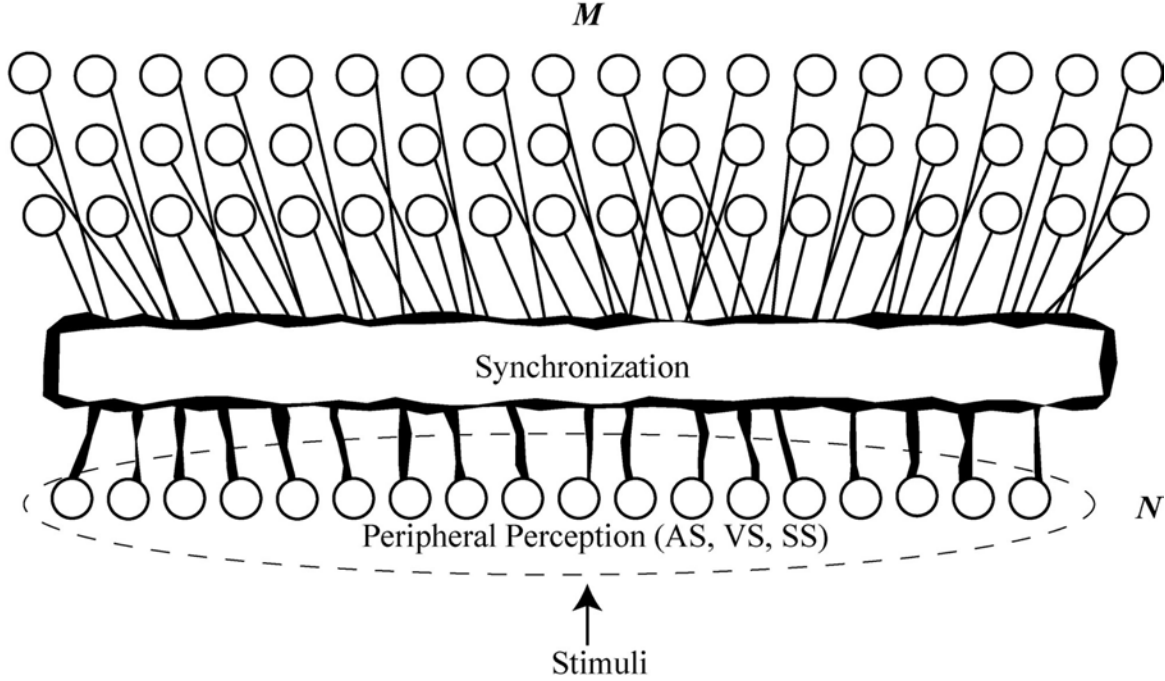


Figure 8. General architecture: illustration of the basic concept of sparsely synchronized activity. The peripheral sensory organ, i.e., retina (VS), cochlea (A.S), or skin (S.S.) uses a nonsparse representation of stimuli (place coding) encoded with N neurons (layer N). This representation is then transformed into a sparsely synchronized representation at higher levels of the brain with M neurons (where M is much higher than N). The transformation requires synchronization of the inputs to elicit a response of a small subset of the M neurons. The peripheral encoding is based on place coding; it is nonsparse and the respective activity of each N individual neuron is strongly correlated with the other N neurons. On the other hand the activity of each M output neuron is weakly correlated with the other M neurons. Furthermore, the M neurons are sparsely synchronized.

5.1. Formal Model of an Isolated Neuron

It is possible to derive general equations that account for cellular responses from which transient and sustained responses can be further investigated in order to integrate the above proposals into a general model. The neuron model we use is the conventional simplistic integrate and fire neuron. Real neurons are much more complex with a richer dynamic. But the integrate and fire spiking neuron can reproduce some of the characteristics of subsets of real neurons. Therefore, there is a great probability that the proposed model behavior can be observed in brains. The sub-threshold potential $v(t)$ of a simplified integrate and fire neuron with a constant input is:

$$\frac{dv(t)}{dt} = -\frac{1}{\tau}v(t) + \frac{1}{C}I_0 \quad (4)$$

$v(t)$ is the output electrical potential, I_0 is the input current. When $v(t)$ crosses, at time t_{spike} , a predetermined threshold θ , the neuron fires and emits a spike $AP(t_{spike})$. Then $v(t)$ is reset to V_o . C is the membrane capacitance, τ has the dimension of a time

constant expressed in seconds. After integration, the final expression of $v(t)$ is

$$v(t) = \frac{I_0}{C} \left(1 - e^{-\frac{t}{\tau}}\right) \quad (5)$$

and we assume that the initial instant t_0 is equal to 0.

The neuron that is described by equation (5) can oscillate. When the membrane potential $v(t)$ of a neuron (i, j) becomes, at time t_{spike} , equal or greater than the internal threshold θ , the neuron shall fire generating a spike:

$$x(i, j; t_{spike}) = AP(t) * \delta(t - t_{spike}) \quad \text{if } v(t_{spike}) \geq \theta \quad (6)$$

otherwise $x(i, j; t) = 0$. After firing, the membrane potential $v(t_{spike}^+)$ is reset to V_o . $AP(t)$ is the action potential (usually assumed to be equal to 0 when $t < 0$

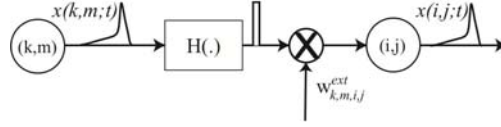


Figure 9. Details of a connection from neuron (k, m) projecting into neuron (i, j) in another layer. The initial action potential $AP(t_{spike})$ is squared by the $H(\cdot)$ transform and then multiplied with weight w . This simplifies the simulation while preserving the aptitude of the neural network to perform binding by synchronization.

and having an impulsive waveform with a finite duration), $*$ is the convolution, $\delta(t)$ is the Dirac impulsions¹ function and

$$t_{spike}^+ = \lim_{\varepsilon \rightarrow 0} (t_{spike} + \varepsilon) \quad (8)$$

The above relations express the rhythmic behavior of a single cell. In fact, if $\frac{I_o}{C}$ in equation 5 is

greater or equal to θ then the neuron can oscillate even if the neurons it is connected to are not active². The phase and the frequency of the oscillations will depend on the activity

of cells to which it is connected. On the other hand if $\frac{I_o}{C}$

is smaller than the internal threshold θ then, to fire the neuron has to be part of a network³.

5.2. The neuron inside a neural network

Now, let us consider neurons that are connected to other cells. We use two types of connections: local for neurons inside the same layer and global connections between neurons being in different layers. An example of this is given on Figure 13. Also, instead of manipulating action potentials the model is built around impulses as illustrated in Figure 9.

For an example, Figure 13 illustrates the connectivity pattern between a neuron (i, j) and 3 neurons (k, m) . One neuron (k, m) is on the same layer and the two other neurons (k, m) are located on other layers. Connections are bi-directional.

5.3. Contribution from the other neurons

Connecting neurons together and writing the general equation that describes the network behavior is our next aim. Let us assume that a neuron (i, j) is connected to other neurons and that it receives a total contribution $S_{i,j}(t)$ from the other neurons it is connected to (neurons $(k, m)^{int}$ from the same layer, neurons $(k, m)^{ext}$ from the other layers, and inhibition - crudely modeled here as a global inhibitor. We use, as a notation, the cardinal position of a neuron in the layer plane. Neuron (i, j) is located in

row i and column j , and neuron (k, m) may be any neuron connected to neuron (i, j) in the same or in another layer. At some time t , the contribution $S_{i,j}(t)$ from all neurons in the neural network to neuron (i, j) is

$$S_{i,j}(t) = \sum_{k,m \in N^{ext}(i,j)} \{w_{i,j,k,m}^{ext} H(x^{ext}(k, m; t))\} + \sum_{k,m \in N^{int}(i,j)} \{w_{i,j,k,m}^{int} H(x^{int}(k, m; t))\} - \eta G(t) \quad (9)$$

where $w_{i,j,k,m}^{ext}$ are the connecting weights between neuron (i, j) and neurons (k, m) , with neuron (i, j) and neurons (k, m) being in a different layer. $w_{i,j,k,m}^{int}$ are the connecting weights between neuron (i, j) and neurons (k, m) inside the same layer. $H(\cdot)$ is the function where $H(x(k, m; t))$ equals 1 if and only if $x(k, m; t) > 0$. $x(k, m; t)$ is the spike output from neurons (k, m) . The first term in the right-hand side of equation (9) is the total contribution coming from all neurons in external layers; the second term is the total contribution coming from all neurons in the same layer as neuron (i, j) , and the last term is the contribution from the global inhibitor.

The inhibitory influences are integrated into one global inhibitory controller $\eta G(t)$. η is a constant that weights the global inhibitor controller contribution. We assume that this inhibitor is connected to all neurons. Its membrane potential $u(t)$ follows the equation:

$$\frac{du(t)}{dt} = -\zeta u(t) + \sigma \quad (10)$$

It is a leaky integrator that is leading ($\sigma = 1$) only if the global activity of the network is higher than a predefined threshold Θ , otherwise $\sigma = 0$ in equation 10⁴. The final expression for a neuron (i, j) inside the network becomes

$$\frac{dv_{i,j}(t)}{dt} = -\frac{1}{\tau}v_{i,j}(t) + \frac{1}{C}I_o + S_{i,j}(t) \quad (12)$$

τ , C are the same variables as in equation 5, I_o is the external input to the neuron (for example: stimulus) and $S_{i,j}(t)$ is the total contribution coming from the other neurons of the network as given in equation 9.

5.4. Expressing the connection weights

The synaptic weight depends on the similarity between features. That is, the closer the features, the stronger the synaptic weights should be. Conversely, neurons characterizing dissimilar features should exert a weak influence and should have small synaptic weights. This is in accordance with the Hebbian learning rule. Although the Hebbian learning rule yields equilibrium and stabilization of the synaptic weights through self-organization of the network, it requires time. We bypass this step by setting up the weights depending on the stimulus inputs (equation 13). In principle this procedure is faster than using the Hebbian rule. Another advantage of this approach is that the designer can encode the network behaviors into the weights. It is then possible to assign strong weights between two visual features of targets moving in opposite directions.

The connecting weights have the general form:

$$w_{i,j,k,m}^{int} = \frac{w_{max}^{int}}{Card\{N^{int}(i,j)\}} \cdot e^{-\lambda|i_{i,j}(t)-i_{k,m}(t)|} \text{ for intra-layer connections} \quad (13)$$

$$w_{i,j,k,m}^{ext} = \frac{w_{max}^{ext}}{Card\{N^{ext}(i,j)\}} \cdot e^{-\lambda|i_{i,j}(t)-i_{k,m}(t)|} \text{ for extra-layer connections}$$

$w_{i,j,k,m}^{int}$ are connections inside the same layer. $w_{i,j,k,m}^{ext}$ are connections between two different layers (neurons (i,j) and (k,m) do not belong to the same layer). w_{max}^{ext} , w_{max}^{int} and $Card\{N^{int}(i,j)\}$, $Card\{N^{ext}(i,j)\}$ are normalization factors. $e^{-\lambda|p(i,j;t)-p(k,m;t)|}$ can be interpreted as a measure of the difference between inputs of neurons (i,j) and (k,m) , i.e., the difference between local properties of trigger features that activate both cells. For instance it may be two orientations characterizing the same image. Here $i_{i,j}(t)$ and $i_{k,m}(t)$ are respectively external inputs to *neuron* (i,j) and *neuron* (k,m) . *neuron* (k,m) is physically connected with neuron *neuron* (i,j) . One defines $N^{ext}(i,j)$ as the set of neurons connected to neuron (i,j) that are not on the same layer as neuron (i,j) . $N^{int}(i,j)$ is the set of neurons connected to neuron (i,j) that are on the same layer as neuron (i,j) . $Card\{N(i,j)\}$ is equal to the cardinal number (number of elements) of the set $N(i,j)$ containing all

neurons connected to the *neuron* (i,j) (it comprises all neurons connected to (i,j) whether they are in the same or different layers). Therefore, $Card\{N(i,j)\} = Card\{N^{ext}(i,j) \cup N^{int}(i,j)\}$.

In summary, we have presented and implemented a model that is used to illustrate next sections and our superposition principle.

6. OBJECTS REPRESENTATIONS

We first describe how sub-populations of neurons that are binded with synchronization remain synchronized even if they are affine transformed of each others. To ease the understanding we illustrate the principle on images where features are based on image pixel's structures. It must be kept in mind that, in the brain, much more complex features are binded all-together. The proposed synchrony model refers to a potential central processing and not to peripheral. Second, we present our affine superposition model principle as a potential representation of objects in the brain. Again, illustrations of our model are given for visual stimuli, but the same principle applies to auditory and other sensory stimuli.

6.1. Feature Extractions: Illustration with Image

An object may be represented by a set of active neurons (points) corresponding to appropriate trigger features exciting responsive neurons. This principle is illustrated in Figure 10. Eight responsive neurons (written as $T1, T2, \dots, T8$) are selectively sensitive to eight features belonging to an image of a car. Each responsive neuron fires only if its inputs are synchronized. Coming back to Figure 8, these neurons could fit in layer M with distinctive receptive fields being obtained from the synchronization of a great number of neurons in layer N .

In Figure 10, the synchronized inputs to each respective Ti responsive neurons are illustrated. Responsive neurons are in layer M and input neurons cluster in subsets defined by synchronous occurrence of firing. Each Ti responsive neuron in layer M receives synchronized inputs (from neurons in a lower layer) with the same time lag from a subset of neurons firing synchronously at Ti . As an example, neuron $T2$ receives synchronized inputs at time lag $T2$ and its synchronous input neuron subset roughly signals the body of a car. Neuron $T2$ can also receive inputs from neurons firing at other time, Tj with $j \neq 2$ but it will not fire as it selectively spikes only when the number of neurons firing at $T2$ is high enough. In this example the features reflected in the neuronal activities are typical of a car body, the contour, the car windows and the image background. The fact that only these eight sparsely distributed neurons fire signifies that the underlying object

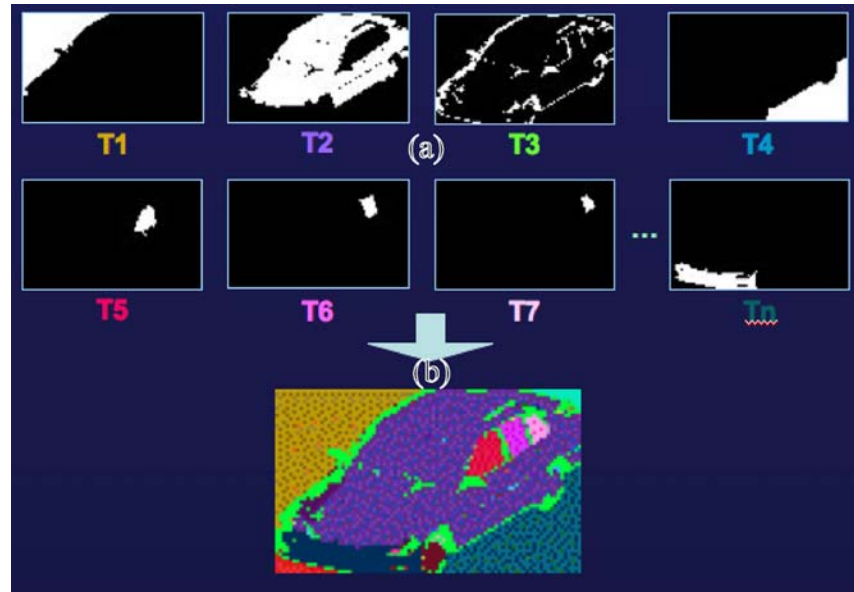


Figure 10. Object as a set of feature responsive neurons. Each feature is encoded in the respective receptive field of eight neurons. One output feature neuron (denoted as T_i) responds only when the neurons in the input layer fire in synchrony and according to a structure (typical of the feature) that follows the receptive field of neuron T_i . (a) : Receptive fields from neurons T_1 to T_8 ; (b) : The superposition of activity of the feature responsive neurons builds the image of a car. In (a), each active neuron from an input feature is colored in white; in (b) a different color is used to illustrate the receptive fields of the 8 T_i neurons. This image has been generated with the model described in section 3 with one layer of neurons for the segmentation and an output layer comprising the 8 T_i neurons (with no intra-layer connections). Gray levels of the pixels are the inputs to the first layer. Each pixel is associated to one neuron in the first layer. For illustration purposes, neurons firing at the same instant are illustrated with the same color. The first layer of the neural network ‘segments’ the input image of a car, while the neurons in the output layer (2nd layer) represent the 8 features associated to each ‘segment’. To save space, only the instants of spiking are illustrated on the figure, the original gray-scale image of the car is not shown here.

(car) can be described by the eight features that typically excite the eight underlying T_i neurons.

In this experiment, neurons in the input layer that are in synchrony characterize the same feature. The synchrony in the input layer arises following the activity of local connections $w^{int}_{i,j,k,m}$. These connections are symmetrical. Also, with this example based on image pixels, input neurons are bound together if pixel’s value are close or similar. This give birth to segment’s based features. The synchrony between neurons T_1 to T_8 is not illustrated here. For instance T_2 and T_3 may be bound together as they share a common characteristic (that is a car shape) and consequently discharge together.

6.2. Binding and affine transformations

An interesting characteristic of the binding, we are looking for here, is the possibility of associating (binding) subnetworks through affine transforms. In this context two sub-populations of neurons remain in synchrony even if their firing patterns are affine transformed of each others. The affine transformation is an efficient way of representing a single object regardless of some deformations or variations of the object (rotation, translation, size and shearing).

As a typical example, the organization of visual cortex may be, and often it is the case, viewed as

hierarchical, with progressive changes from small RFs, with simple response properties in early visual areas, to larger RF and responses governed by more complicated or abstract criteria in later processing stages (105-107). In brain, the processing of visual information takes place in the occipital, temporal and parietal cortices. Up to 32 cortical zones were identified, as their neurons are responsive to visual stimuli (14). The retinal surface that has a visuotopic organization is maintained along this path. The sole exception seems the MT area which is a non-topographically organized visual area (21). Thus, even when the functions may differ within respective area, the retinotopy is preserved, in each individual area to the next that is there is co linearity between retinal points in each respective cortical area. Although receptive fields be may larger in anterior cortical areas the ratio of distances between retinotopic points is maintained (105), which is typical of an affine transform. Then such topographic organization allows the opportunity of applying affine transformation of cortical maps

6.3. A neural network binding insensitive to affine transforms

An affine transformation is a mapping function between two affine spaces that consists of a linear transformation (rotation, scaling or shearing) followed by a translation (Figure 11). Other authors will obtain an affine

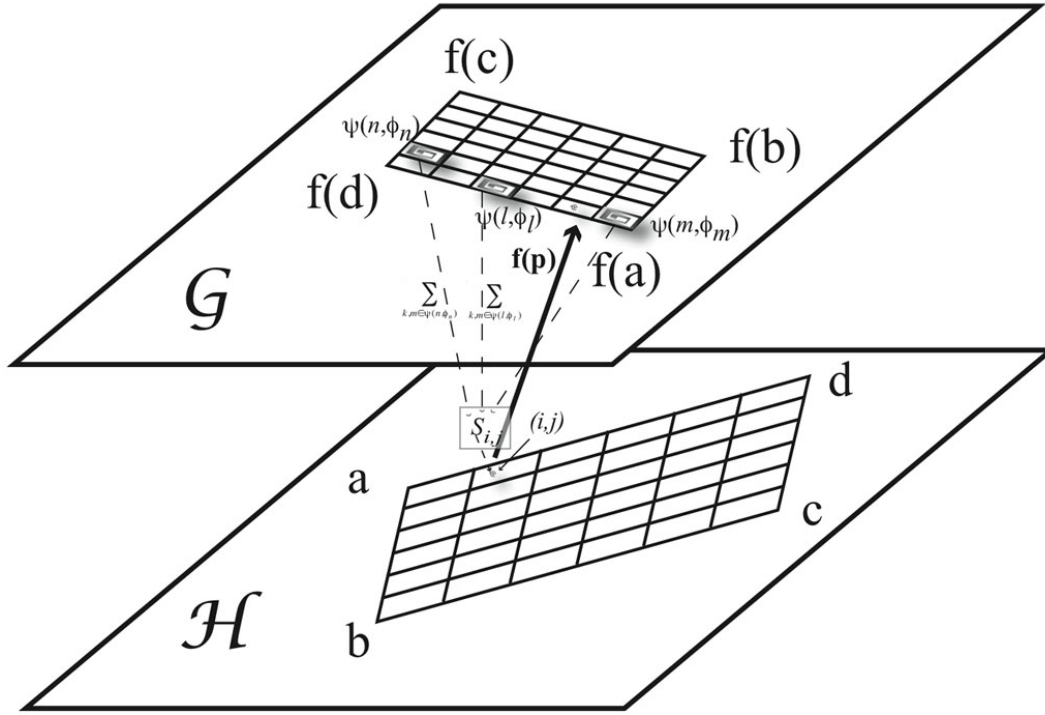


Figure 11. Affine transformation between spaces H and G: The object $\{f(a), f(b), f(c), f(d)\}$ in G is affine transformed from object $\{a, b, c, d\}$ in H. Both objects are illustrated as made of contiguous compact parts.

transformation by combining a scaling transformation with an isometry or a shear with an homothety and an isometry. In our hypothesis affine transformations could map two cortical regions or two associative areas while preserving the synchronization of the binding.

For the sake of simplicity we make our demonstration in two dimensional spaces, but it can be easily generalized. An object can be represented by a set of points corresponding to its corners (Figure 11) and a set of compact constituents being inside the surface defined by the corners. Any affine transform is a map f from one space H to another one G, both of them being in R^2 . In Figure 11 each layer H or G is a subset of R^2 . An affine transform $f: H \rightarrow G$ maps each point from one layer to another with :

$$f(p) = A * p + Shift \quad (1)$$

Where A is a 2x2 non-singular matrix, p is a point in the input plane (i.e. neuron (i,j) in layer H), and $f(p)$ is its affine transform. $Shift$ is the translation vector.

Now suppose that the object $\{a, b, c, d\}$ from layer H is mapped by the affine transform f to the subset $\{f(a), f(b), f(c), f(d)\}$ from layer G. We show here that the contribution $S_{i,j}$ received by neuron (i,j)

being inside layer H is independent of any affine transformation f because of the normalization factors $Card\{N(i,j)\}$ from the connecting weights $w_{i,j;k,m}^{ext}$ as expressed in equation (9).

Let us come back to the total contribution to neuron (i,j) :

$$S_{i,j}(t) = \sum_{k,m \in N^{ext}(i,j)} w_{i,j;k,m}^{ext} H(x^{ext}(k,m;t)) + \sum_{k,m \in N^{int}(i,j)} w_{i,j;k,m}^{int} H(x^{int}(k,m;t)) - \eta G(t)$$

The expression

$$\sum_{k,m \in N^{int}(i,j)} w_{i,j;k,m}^{int} H(x^{int}(k,m;t)) - \eta G(t) \quad \text{is}$$

independent of the affine transform f as it depends only on the internal connections and of the global controller. Therefore, in the remaining part, we only consider extra-connections between both layers. The extra layer contribution maybe written as:

$$S_{i,j}^{Ext}(t) = \sum_{k,m \in N^{ext}(i,j)} \frac{w_{i,j;k,m}^{ext} e^{-\lambda |t_{i,j}(t) - t_{k,m}(t)|}}{Card\{N(i,j)\}} H(x^{ext}(k,m;t))$$

At time t , $S_{i,j}^{Ext}(t)$ depends on the inputs and on the activity of the neurons. Some neurons fire (yielding $H(x^{ext}(k,m;t))=1$) or do not ($H(x^{ext}(k,m;t))=0$).

Instead of writing $S^{Ext}_{i,j}(t)$ as the sum of individual neuron contributions, we now write $S^{Ext}_{i,j}(t)$ as the sum of the contributions coming from all subsets of synchronized neurons. An object is a compact set, partially represented by synchronized subsets of neurons. Let us assume that neurons (k,m) on layer G fire with a phase lag ϕ_l . Because of the dynamics of the neural network, subsets $\psi(l, \phi_l)$ of synchronized neurons appear on layer G. M is the number of these subsets. At time l , neurons (k,m) belonging to the same subset $\psi(l, \phi_l)$ fire in synchrony (with a phase lag of ϕ_l), while others (k,m) will not as they do not belong to the same subset characterize by the ϕ_l phase lag. If we spatially integrate the contribution coming from all neurons -- that is, we add all contributions, assuming that each neuron from layer G has fired one spike -- we may now write

$$S^{Ext}_{i,j} = \sum_{l=1}^M \left(\sum_{k,m \in \psi(l, \phi_l)} \frac{w_{\max}^{ext}(t) e^{-\lambda|i_{i,j}(t) - i_{k,m}(t)|}}{Card\{N(i,j)\}} \right)$$

Neurons firing with the same phase ϕ_l have similar input features. Therefore, to a first approximation, we can assume that the expression $e^{-\lambda|i_{i,j}(t) - i_{k,m}(t)|}$ is the same for neurons belonging to the same firing subset $\psi(t, \phi_l)$. We note as $similarity(\phi_l)$ the approximation of $e^{-\lambda|i_{i,j}(t) - i_{k,m}(t)|}$ when neurons (k,m) , on layer G fire with the same phase ϕ_l .

$$similarity(\phi_l) = e^{-\lambda|i_{i,j}(t) - i_{k,m}(t)|}$$

The greater the $similarity(\phi_l)$, the better is the concordance between the external input of neuron (i,j) and those of neurons (k,m) . We also write as $(\Delta_{\phi_l})^G$ the number of neurons (k,m) in layer G that fire in synchrony with the phase ϕ_l . In other words $(\Delta_{\phi_l})^G$ is the number of neurons belonging to the same subset $\psi(t, \phi_l)$ from layer G. We then obtain.

$$S^{Ext}_{i,j} \cong \sum_{l=1}^M \frac{(\Delta_{\phi_l})^G w_{\max}^{ext}(t)}{Card\{N(i,j)\}} similarity(\phi_l)$$

Let us recall that $Card\{N(i,j)\}$ is the total number of active connections between neuron (i,j) and all other neurons (k,m) whether they are on layer H or G. As the typical number of local active connections is relatively small (on the order of ten's) while the typical number of connections between the layers is on the order of thousands; we, then, approximate $Card\{N(i,j)\}$ as being the number of all extra-layers neurons (k,m) connected to neuron (i,j) . That is:

$$Card\{N(i,j)\} \sim \sum_{k=1}^M (\Delta_{\phi_k})^G$$

Thus, $S^{Ext}_{i,j}$ becomes:

$$S^{Ext}_{i,j} \cong w_{\max}^{ext}(t) \sum_{l=1}^M \frac{(\Delta_{\phi_l})^G}{\sum_{k=1}^M (\Delta_{\phi_k})^G} similarity(\phi_l)$$

This relation shows that $S^{Ext}_{i,j}$ is a weighted sum of all $similarity(\phi_l)$ where $\frac{(\Delta_{\phi_l})^G}{\sum_{k=1}^M (\Delta_{\phi_k})^G}$ is the ratio

between the size of the firing cluster $\psi(t, \phi_l)$ and the total size of the synchronized neurons on layer G. We also know that any affine transform f from layer H to G preserves the relative proportion between parts of objects:

$$\frac{(\Delta_{\phi_l})^G}{\sum_{k=1}^M (\Delta_{\phi_k})^G} = \frac{(\Delta_{\phi_l})^H}{\sum_{k=1}^M (\Delta_{\phi_k})^H}$$

This yields a new expression of the contribution that is independent of the size of the areas (size of the subsets of synchronized neurons) in layer G:

$$S^{Ext}_{i,j} \cong w_{\max}^{ext}(t) \sum_{l=1}^M \frac{(\Delta_{\phi_l})^H}{\sum_{k=1}^M (\Delta_{\phi_k})^H} similarity(\phi_l)$$

This means that the extra-layer connections are independent of the affine transform f that maps subset of synchronized neurons from one layer to another one.

From this model we can conclude that the binding by synchronization is insensitive to affine transforms. Thus, if two objects, are initially binded by synchronization and if the shape of one of the object is affine transformed at some time, the binding will remain valide for the type of neural network we propose here. We have done two assumptions : Each neuron should have fire one spike and two synchronized neurons have similar feature values. These assumptions seem reasonable in the context of a synchronized neural network implementing the binding.

6.4. Binding, affine transformations and synchroniation

The binding, based on firing rates has already been proposed by Knoblauch *et al.* (51). But, as discussed previously, rate-based binding between neural subnetworks is a relatively slow process while spike-based binding is much faster. Figure 2 illustrates how binding between two neuronal sub-populations can change in few cycles. One

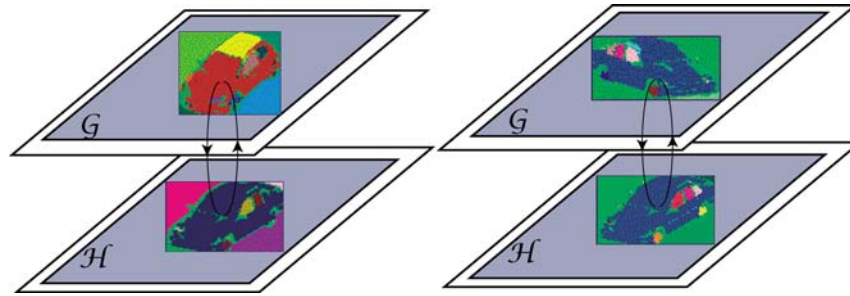


Figure 12. Binding between neuronal populations: Arrows illustrate connections between both layers. Illustration by superposition of the activities of the feature responsive neurons. The colors represent the various neuronal populations firing in synchrony (with a different color to characterize neurons firing at different time lags). Left: the 2 sets of neuronal feature populations are not affine transformed of their respective input activities, the matching index is approximately equal to 15% (i.e. the two car images are not affine transformed of each others). Right: both sets are fully synchronized, as the 2 populations (illustrated here as 2 layers of neurons) have activities that are approximately affine transform's of each others (i.e the two car images correspond to a same car model); the matching index equals 95%. Note that, the neural network model is insensitive to the orientation of the cars (that is a fundamental property of affine transforms). This images have been generated with the model described in section 3 with two layers of neurons. Gray levels of the pixels are the inputs. Each pixel is associated to one neuron. To save space, only the instants of spiking are illustrated with a color code for the instant of spiking. The original gray-scale images are not shown here.

contribution from the model by Pichevar et al., (108, 109) has been to propose a solution to the binding between populations of neurons based on the synchronization between spiking neurons. Figure 12 displays the results of the proposed binding neural network where two images of cars are compared with a two layered neural network (one image on each layer is presented). When the cars are different (first row of Figure 12), few neurons synchronize across the two layers. The second row shows that the comparison of the same car model yields a maximum synchronization between both layers (both layers share the same instants of discharges : same colors between the two layers).

Coming back to the computer simulations from Figures 2 and 10, neurons that are in synchrony characterize the same feature. Even if these features belong to different neuronal subnetworks the simultaneous activation of respective cells may result in swift coordination of cellular activity. In addition, synchronized activity could be very selective, for instance the two illustrated networks synchronize exclusively for local features. This example may of course be extended by adding supplementary properties.

Along these lines Rouat et al. (108-111), showed that a pattern may be identified by a matching procedure and the estimation of a synchronization index r :

$$r = S_m / S_t \quad 100\%$$

S_m is the total number of neurons activated by trigger features that produce the same synchronization, while S_t is the total number of neurons in the network. Hence r represents the proportion of synchronized active cells. In Figure 12, r is approximately equal to 15% for the image matching with 2 different cars, and 95% for the image matching with the same car.

Our proposal is shown in Figure 13. Three layers (three matrices of neurons) are superimposed. Each layer comprises clusters of cells activated by one or two trigger features (for example in Figure 13, each cell is initially activated by orientation or color or motion). Of course these trigger features are present simultaneously. These units synchronize within their respective layer in relation with the topic structure of the feature when the stimulus is present in the subject's environment. A different stimulus would yield a different activity pattern inside each layer. This activity pattern is dependent on the feature representation for the stimulus. For a particular layer (e.g., the orientation layer), a different stimulus would generate a different pattern of activity inside that feature (orientation) layer. The same occurs for the other layers. We assume that each layer preserves the topic structure of the relevant sensory input (i.e., tonotopic for audition, retinotopic for vision etc.). Therefore a given stimulus produces, in the feature layers, patterns of activity that are assumed to be affine transformations of each other. The affine transformation preserves the cellular relationships between features and transfers activities between layers. Furthermore, it is possible to link all layers to form one single synchronized neuronal assembly which would represent the object in its integrity. In addition several linear transformations may be combined into a single one so that the general principle is still applicable.

Since synchrony of activity between neurons is related to stimulus properties, it seems logical to postulate that such binding by synchrony is not ubiquitous (55, 112-116). Indeed, only cells that are excited by specific features can potentially synchronize. The formation of such a neuronal assembly is specific to this combination of properties. As a consequence feature extraction is facilitated. Also, only the sub-population characteristic of the actual object stimuli is fully synchronized. Since other

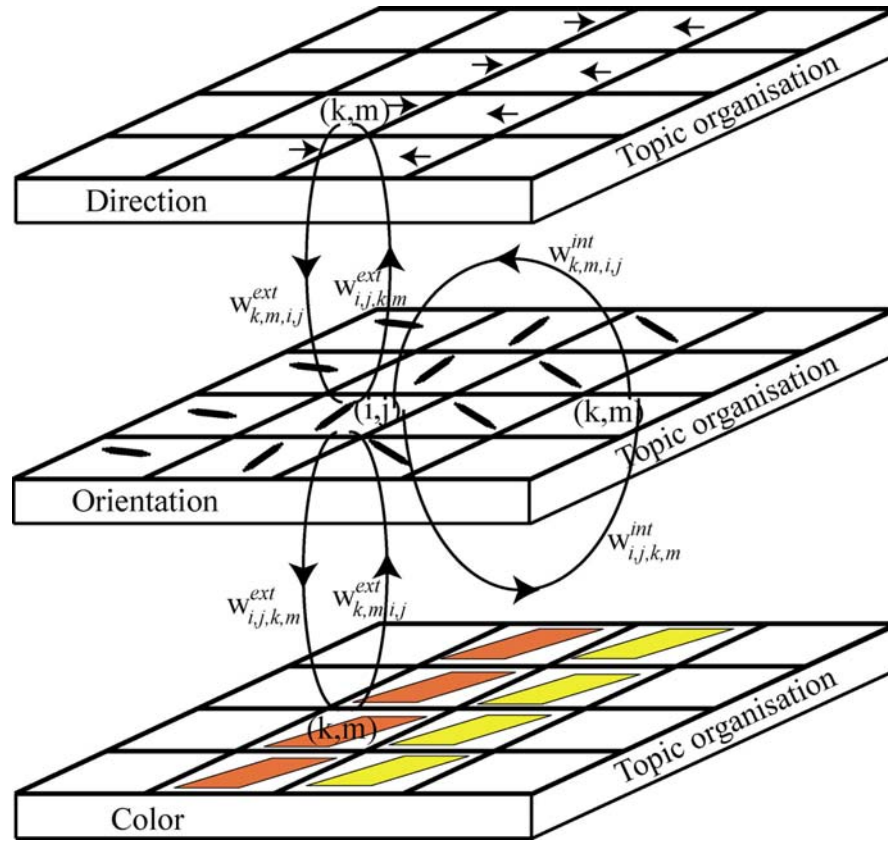


Figure 13. Binding between features of an object via time correlation. Three neuronal layers are illustrated. Each layer preserves the topic organisation of the sensory sub-system under consideration (i.e., vision in this example). The first layer comprises neurons that respond to direction of the movements, the second layer characterizes orientation and the third color. Neurons inside a layer are locally connected with symmetrical connections. Between layers connections are also bi-directional and symmetric with full connections. The binding process acts as a ‘segmenter’ inside layers. Between layers, binding is used to match groups of neurons through layers. The Figure illustrates one local connection inside the orientation layer between neurons (i,j) and (k,m) and two extra-layer connections between the same neuron (i,j) from the orientation layer and two neurons (k,m) respectively from the color and direction layers.

neurons will not synchronize, it is justified to suggest a sparse synchronized activity.

The model, simultaneously captures both the stimulus dependence on features and detailed spatio-temporal correlations in population responses, and provides two insights into the structure of the neural code. First, neural encoding at the population level is less noisy than one would expect from the variability of individual neurons as spike times are more precise, and can be predicted more accurately when the spiking of inter- or intra- layer neurons is taken into account. Second, time correlations provide additional sensory information: optimal, model-based decoding that exploits the response correlation structure. It may extract a large amount of information about the visual or auditory scenes. This model-based approach reveals the role of correlated activity between cells coding sensory scenes, and provides a general framework for understanding the importance of correlated activity in populations of neurons, regardless of their positions.

7. CONCLUSIONS: SPARSNESS AND SUPERPOSED NEURONAL ASSEMBLIES

Superposed assemblies present several advantages over serial or hierarchical streams of information:

1. The probability of large numbers of cells exhibiting simultaneous synchronized activity becomes smaller as the number of units increases. Since only synchronizing cells are contributing to encoding, their number is relatively small which appears to be economical.
2. In a serial stream of coding the propagation of stimulus-related responses results in loss of temporal accuracy, partially due to latency jitters in response to relatively weak stimuli, whereas synchrony within a 1 ms time-window offers better precision. Indeed, a small perturbation or change in the stimulus modifies the timing of action potentials. The consequence is an alteration of the neuronal

assembly resulting in a disturbance of the encoding process, thereby increasing selectivity.

3- Sparse synchronization coding contributes to reduced redundancy observed at peripheral levels.

4. A superposed assembly provides the possibility to assign features from multiple sources, for instance auditory and visual, etc., yet each assembly maintains its individuality as it is initially created by the presence of particular traits belonging to one object. Hence a functional segregation reduces ambiguities since assembly may co-exist and switch from one to another.

5. A synchronization within ~1ms time windows permits a high degree of flexibility since it is feasible to shift rapidly from one to another one. For instance partial decorrelation or additional correlation allows jumping from one sub-network to another one. This is quick because of this short time scale. These changes in correlated activity might reflect changes in the functional of a neuronal circuit.

6. Along this line because synchrony occurs within a very short time-window the refresh rate is rapid. That is the previous stimuli does not persist thereby allowing a prompt reset of neuronal network.

7. A functional model based on synchrony may facilitate plasticity that involves modifications of synaptic relationships between cells. Since sparseness rests on synchronous action potentials it is suitable for Hebbian modifications of synaptic balance. Particularly spike-timing-dependent plasticity or STDP.

8-. Multiplexing augments the encoding capacity of neuronal responses and at the same time allows disambiguation of stimuli that appears in the subject's environment

9- Yet such a model poses several problems. Sparseness by definition rests on a discontinuous or fractioned organization of activity which seems to be counterintuitive with the regular and coherent flow in everyday perception.

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Footnotes

¹The Dirac function has the property that

$$\mathbf{AP}(t_{spike}) = \mathbf{AP}(t) * \delta(t - t_{spike}) \quad (7)$$

²These neurons are sometimes called *leaders*.

³These neurons are sometimes called *followers*

⁴One defines the global activity of a neuronal network as

$\sum_{k,m \in N(G)} [w_{k,m,G} H(x(k,m;t))]$ with $N(G)$ the set of all neurons connected to the global controller (that is here all neurons from the network) and $w_{k,m,G}$ the connection from neuron (k,m) to the global controller G .

$$\text{If } \sum_{k,m \in N(G)} [w_{k,m,G} H(x(k,m;t))] \geq \Theta$$

Then, $\sigma = 1$ in equation (10); otherwise, $\sigma = 0$ in equation (10).

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